| Hi-Tech Institute of Engineering \& Technology |  |
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| DEPARTMENT OF COMPUTER SCIENCE \& ENGINEERING |  |
| MODEL TEST PAPER I, ODD SEMESTER-2023-24, |  |
| Semester: 3rd | Course/Branch: CS/IT/AI-ML |
| Subject Code:BAS303 | Subject Name: MATHEMATICS IV |
| Faculty Name: SHIVANI SHUKLA |  |
| Time: 3: 00 Hours | Total Marks: 70 |

Note: Attempt all Sections. If you require any missing data, then choose suitably.

## SECTION A

1. Attempt all questions in brief.

2X7=14

| Q No. | Question |  |  |  |  |  |  | Marks | CO |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| a. | From partial differential equations of the equations by eliminating the arbitrary constants: $z=a x+b y+a b$ |  |  |  |  |  |  | 2 | 1 |
| b. | Solve: $\left(D^{3}-4 D^{2} D^{\prime}+4 D D^{\prime 2}\right) z=0$ |  |  |  |  |  |  | 2 | 1 |
| c. | Write the wave equation in two dimensions. |  |  |  |  |  |  | 2 | 2 |
| d. | If $P(A)=\frac{1}{4}, P(B)=\frac{1}{2}, P(A \cup B)=\frac{5}{8}$, find the value of $P(A \cap B)$. |  |  |  |  |  |  | 2 | 4 |
| e. | Find the arithmetic mean of the following frequency distribution: |  |  |  |  |  |  | 2 | 3 |
|  | $\mathbf{x}$ $\mathbf{1}$ | 2 | 3 | 4 | 5 | 5 | 7 |  |  |
|  | $y$ 5 | 9 | 12 | 17 | 14 | 10 | 6 |  |  |
| f. | Define Alternative Hypothesis. |  |  |  |  |  |  | 2 | 5 |
| g . | What do you mean by "statistical quality control (SQC)"? |  |  |  |  |  |  | 2 | 5 |

## SECTION B

2. Attempt any three of the following:

7X3=21

| Q No. | Question |  |  |  |  | Marks | CO |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| a. | Solve the following partial differential equation by using the method of separation of variables:$\frac{\partial z}{\partial x}+\frac{\partial^{2} z}{\partial y^{2}}=0 ; z(x, 0)=0, z(x, \pi)=0, z(0, y)=4 \sin 3 y$ |  |  |  |  | 7 | 2 |
| b. | Solve $\left(x^{2}-y^{2}-y z\right) p+\left(x^{2}-y^{2}-z x\right) q=z(x-y)$. |  |  |  |  | 7 | 1 |
| c. | Use the method of least squares to the curve of the form $y=a b^{x}$ to the following data: |  |  |  |  | 7 | 3 |
|  | $\mathbf{X}$ $\mathbf{2}$ | 3 | 4 | 5 | 6 |  |  |
|  | y 8.3 | 15.4 | $33.1$ | $65.2$ | 127.4 |  |  |
| d. | The mean weight obtained from a random sample of size 100 is 64 grm . The S.D. of the weight distribution of the population is 3 grm . Test the statement that the mean weight of the population is 67 grm at $5 \%$ level of significance, Also set up $99 \%$ confidence limit of the mean weight of the population. |  |  |  |  | 7 | 5 |
| e. | Calculate the moment generating function of the discrete Binomial distribution. Also find the first and second moments about the mean. |  |  |  |  | 7 | 4 |

## SECTION C

3. Attempt any one part of the following:

7X1=7

| Q No. | Question | Marks | CO |
| :--- | :--- | :---: | :---: |
| a. | Solve: $x\left(y^{2}+z\right) p-y\left(x^{2}+z\right) q=z\left(x^{2}-y^{2}\right)$ | $\mathbf{7}$ | $\mathbf{1}$ |
| b. | Solve: $2 x+p^{2}+q y+2 y^{2}=0$ | $\mathbf{7}$ | $\mathbf{1}$ |

4. Attempt any one part of the following:

7X1=7

| Q No. | Question | Marks | CO |
| :--- | :--- | :---: | :---: |
| a. | Solve the Laplace equation $u_{x x}+u_{y y}=0, x \in(0,1), y \in(0,1)$ with the <br> condition $u(x, 0)=u(x, 1)=0$ and $u(0, y)=0, u(1, y)=f(y)$ by using the <br> method of separation of variable. | $\mathbf{7}$ | $\mathbf{2}$ |
| b. | Find the Fourier sine transform of $\frac{e^{-a x}}{x}, a>0$. Hence find Fourier sine <br> transform of $(\mathbf{1} / \mathbf{x})$. | $\mathbf{7}$ | $\mathbf{2}$ |

5. Attempt any one part of the following:

7X1=7

| Q No. | Question |  |  |  |  |  |  | Marks | CO |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| a. | The first four moments of a distribution about the value 4 of the variables are -$1.5,17,-30$ and 80 . Find all four moments about mean. Also find kurtosis. |  |  |  |  |  |  | 7 | 3 |
| b. | Fit the curve $p v^{\gamma}=K$ to the following data: |  |  |  |  |  |  | 7 | 3 |
|  | p(kg/cm^2) | 0.5 | 1 | 1.5 | 2 | 2.5 | 3 |  |  |
|  | v (liters) | 1620 | 1000 | 750 | 650 | 520 | 460 |  |  |

6. Attempt any one part of the following:

7X1=7

| Q No. | Question | Marks | CO |
| :--- | :--- | :---: | :---: |
| a. | The number of accidents in a year involving taxi drivers in a city follows a <br> Poisson distribution with mean equal to 3. Out of 1000 taxi drivers, find <br> approximately the number of drivers such that <br> (i) <br> No accident in a year (ii) More than three accidents in a year. <br> (Given $e^{-3}=0.04979$ ) | $\mathbf{7}$ | $\mathbf{4}$ |
| b. | In normal distribution, 12\% of the items are under 30 and 85\% items are <br> under 60. Find the mean and standard deviation. | $\mathbf{7}$ | $\mathbf{4}$ |

7. Attempt any one part of the following:

| Q No. | Question |  |  |  |  |  |  |  |  |  |  | $\underset{s}{\text { Mark }}$ | C 0 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| a. | Distinguish between the np-chart and p-chart. Following is the data of defectives of $\mathbf{1 0}$ samples of size 100 each. Construct np-chart and examine whether the process is in statistical control |  |  |  |  |  |  |  |  |  |  | 7 | 5 |
| b. | The score of 10 candidates obtained in tests before and after attending some coaching classes are given below: |  |  |  |  |  |  |  |  |  |  | 7 | 5 |
|  | Befor | 54 | 76 | 92 | 65 | 75 | 78 | 66 | 82 | 80 | 78 |  |  |
|  | After | 60 | 80 | 86 | 72 | 80 | 72 | 66 | 88 | 82 | 73 |  |  |
|  | Is the coaching for the test effective? Test at $5 \%$ level of significance. |  |  |  |  |  |  |  |  |  |  |  |  |

